

## 197. Interaction of $\text{Ca}^{2+}$ and $\text{Mg}^{2+}$ with Ionophores Studied by Using a Pair-Potential Model Based on *Ab Initio* Calculations

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### Summary

Atom pair potentials are obtained from *ab initio* SCF-LCAO-MO calculations for model complexes of  $\text{Mg}^{2+}$  and  $\text{Ca}^{2+}$  with *N,N*-dimethylacetamide, *N,N*-dimethylbutyramide and malonamide. The SCF-LCAO-MO interaction energies for 271 complexes of  $\text{Mg}^{2+}$  and 271 complexes of  $\text{Ca}^{2+}$  with these amides were fitted with a simple analytical potential by a least-square procedure. Interaction energies and optimal ion locations obtained by pair-potential calculations are compared with values obtained by *ab initio* calculations for some related amides. The application of the atom pair potentials to the structure of the  $\text{Mg}^{2+}$ -complex  $[\text{MgCl}_2(\text{C}_3\text{H}_7\text{ON})_6]$  of *N*-methylacetamide is discussed.

In view of a design of ionophores with selectivity for  $\text{Mg}^{2+}$  a quantitative treatment of the energy of interaction of ions with ligands is most relevant [1] [2]. Although classical calculations of such interaction energies have given useful hints [1–4], obviously more fundamental computations are necessary for a deeper insight into features of the molecular design [5]. *Ab initio* computations have been successfully applied to assess the interaction of small molecules with various cations [6–8]. For large molecules, *e.g.* realistic ionophores, approximations have been used, which are based on *ab initio* calculations on small molecules [9] [10]. In such an approach ion-ionophore interaction energies have been estimated by an additive procedure as a sum of atom-ion interactions [11] [12] and successfully applied to ionophores such as crown ethers and *N,N,N',N'*-tetracyclohexyl-3-oxapentandiamide [13]. Here we report on the derivation and use of such pair potentials for the interaction of  $\text{Mg}^{2+}$  and  $\text{Ca}^{2+}$  with amides acting as carriers for group Ia and IIa cations [14] [15].

For fixed coordinates of all ligand atoms, pair potentials were derived from interaction energies calculated using the SCF-LCAO-MO approximation for different positions of the ion in the space around the ionophore moiety. The basis sets [16] as applied in previous calculations [11] [12] were used for H-, C-, N- and O-atoms. For  $\text{Mg}^{2+}$  and  $\text{Ca}^{2+}$  those published in [17] were used.

The above interaction energies  $I(L, M)$  ( $L$ : ligand,  $M$ : ion) were fitted using the *Equation 1* [10] [18–20]:

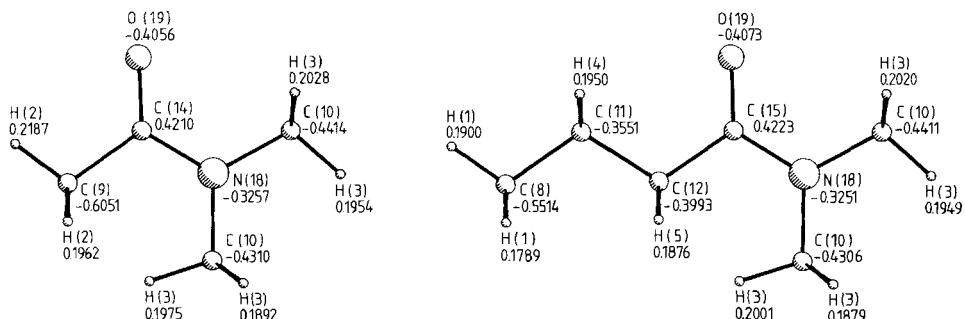
$$I(L, M) = \sum_i (-A_{iM}/r_{iM}^6 + B_{iM}/r_{iM}^{12} + C_{iM} q_i q_M/r_{iM}) \quad (1)$$

where  $A_{iM}$ ,  $B_{iM}$ , and  $C_{iM}$  are adjustable constants,  $r_{iM}$  is the distance between an atom  $i$  on the ligand and  $M$ ,  $q_M$  and  $q_i$  are the net charges of  $M$  and the atom  $i$  calculated for the isolated species. The  $r^{-12}$ -term represents the repulsion between the atom  $i$  and the ion, the  $r^{-6}$ -term a repulsive or attractive interaction (depending on the sign of  $A_{iM}$ ) and the  $r^{-1}$ -term the point charge-point charge interaction, attractive or repulsive depending on the sign of  $q_i$ .  $B_{iM}$  was constrained to be greater or equal  $10^3$  and  $C_{iM}$  greater or equal zero.

Table 1. *Atomic codes and coordinates (in pm) of N,N-dimethylbutyramide*. The geometrical parameters of *N,N*-dimethylacetamide, methyl propyl ether [11] and propionic acid [21] were used. Total energy:  $-362.680108 E_h$ .

| Nr. | Code | X        | Y        | Z       |
|-----|------|----------|----------|---------|
| 1   | H1C1 | 11.415   | -253.376 | 0.000   |
| 2   | C1   | 116.375  | -218.181 | 0.000   |
| 3   | N    | 118.843  | -71.302  | 0.000   |
| 4   | C2   | 247.278  | 0.000    | 0.000   |
| 5   | H1C2 | 330.238  | -73.301  | 0.000   |
| 6   | H2C2 | 254.261  | 63.555   | 90.373  |
| 7   | H3C2 | 254.261  | 63.555   | -90.373 |
| 8   | H2C1 | 167.924  | -256.006 | -90.373 |
| 9   | H3C1 | 167.924  | -256.006 | 90.373  |
| 10  | C3   | 0.000    | 0.000    | 0.000   |
| 11  | O    | -4.355   | 122.427  | 0.000   |
| 12  | C4   | -124.199 | -86.763  | 0.000   |
| 13  | C5   | -254.415 | -4.563   | 0.000   |
| 14  | C6   | -379.409 | -94.505  | 0.000   |
| 15  | H1C6 | -470.355 | -31.384  | 0.000   |
| 16  | H2C6 | -378.930 | -158.440 | -90.373 |
| 17  | H3C6 | -378.930 | -158.440 | 90.373  |
| 18  | H1C5 | -257.811 | 59.284   | 90.373  |
| 19  | H2C5 | -257.811 | 59.284   | -90.373 |
| 20  | H1C4 | -124.612 | -150.700 | -90.373 |
| 21  | H2C4 | -124.612 | -150.700 | 90.373  |

Atoms of the same kind in similar chemical environments (all  $\alpha$ - and  $\beta$ -neighbors having the same atom number and the same hybridization [13]) were grouped in the same classes and have the same constants. The geometries of the molecules for which SCF-LCAO-MO calculations were performed are given in *Tables 1* (*N,N*-dimethylbutyramide) and *2* (malonamide) as well as in *Table 4* of [11] (*N,N*-dimethylacetamide). The corresponding structures are depicted in *Figure 1* together with the atom symbols, class numbers and the net atomic charges. To obtain the pair potentials for the interaction of  $Mg^{2+}$  and  $Ca^{2+}$  with the atoms of the three



N,N-DIMETHYL ACETAMIDE

N,N-DIMETHYL BUTYRAMIDE

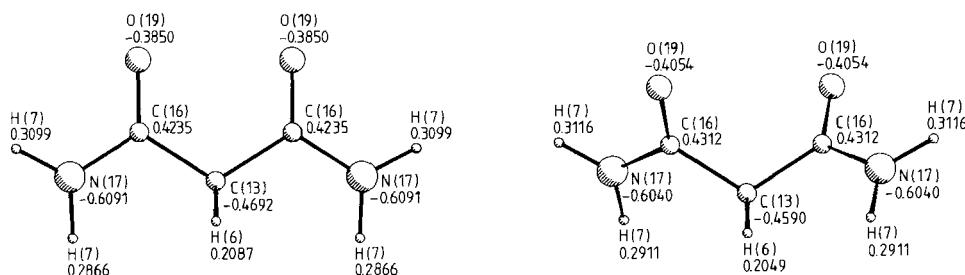
MALONAMIDE,  $\theta_{OCCC} = 0^\circ$ MALONAMIDE,  $\theta_{OCCC} = 45^\circ$ 

Fig. 1. The four structures (two of them different conformations of malonamide) studied for deriving pair potentials for  $Mg^{2+}$  and  $Ca^{2+}$  complexes, atomic symbols, class numbers (in parenthesis) and net atomic charges

Table 2. Atomic codes and coordinates (in pm) of malonamide in the planar conformation (left;  $\theta(OCCC)=\theta(CCCO)=0^\circ$ , total energy:  $-374.369123 E_h$ ) and in the non-planar conformation (right;  $\theta(OCCC)=\theta(CCCO)=45^\circ$ , total energy:  $-374.370918 E_h$ ). The geometrical parameters of acetamide [22] and 1-butene (synperiplanar C-skeleton) [23] were used.

| Nr. | Code | X        | Y        | Z       | X        | Y        | Z        |
|-----|------|----------|----------|---------|----------|----------|----------|
| 1   | H1N1 | -335.056 | -26.595  | 0.000   | -313.914 | 6.463    | -94.736  |
| 2   | N1   | -244.486 | -73.944  | 0.000   | -224.749 | -43.083  | -88.438  |
| 3   | C1   | -127.969 | 0.000    | 0.000   | -127.969 | 0.000    | 0.000    |
| 4   | H2N1 | -240.206 | -176.055 | 0.000   | -207.259 | -124.537 | -147.635 |
| 5   | O1   | -128.820 | 121.997  | 0.000   | -144.966 | 96.751   | 72.350   |
| 6   | C2   | 0.000    | -81.839  | 0.000   | 0.000    | -81.839  | 0.000    |
| 7   | C3   | 127.969  | 0.000    | 0.000   | 127.969  | 0.000    | 0.000    |
| 8   | O2   | 128.820  | 121.997  | 0.000   | 144.966  | 96.751   | -72.350  |
| 9   | N2   | 244.486  | -73.944  | 0.000   | 224.749  | -43.083  | 88.438   |
| 10  | H1N2 | 335.056  | -26.595  | 0.000   | 313.914  | 6.463    | 94.736   |
| 11  | H2N2 | 240.206  | -176.055 | 0.000   | 207.259  | -124.537 | 147.635  |
| 12  | H1C2 | 0.000    | -148.347 | 86.988  | 0.000    | -148.347 | 86.988   |
| 13  | H2C2 | 0.000    | -148.347 | -86.988 | 0.000    | -148.347 | -86.988  |

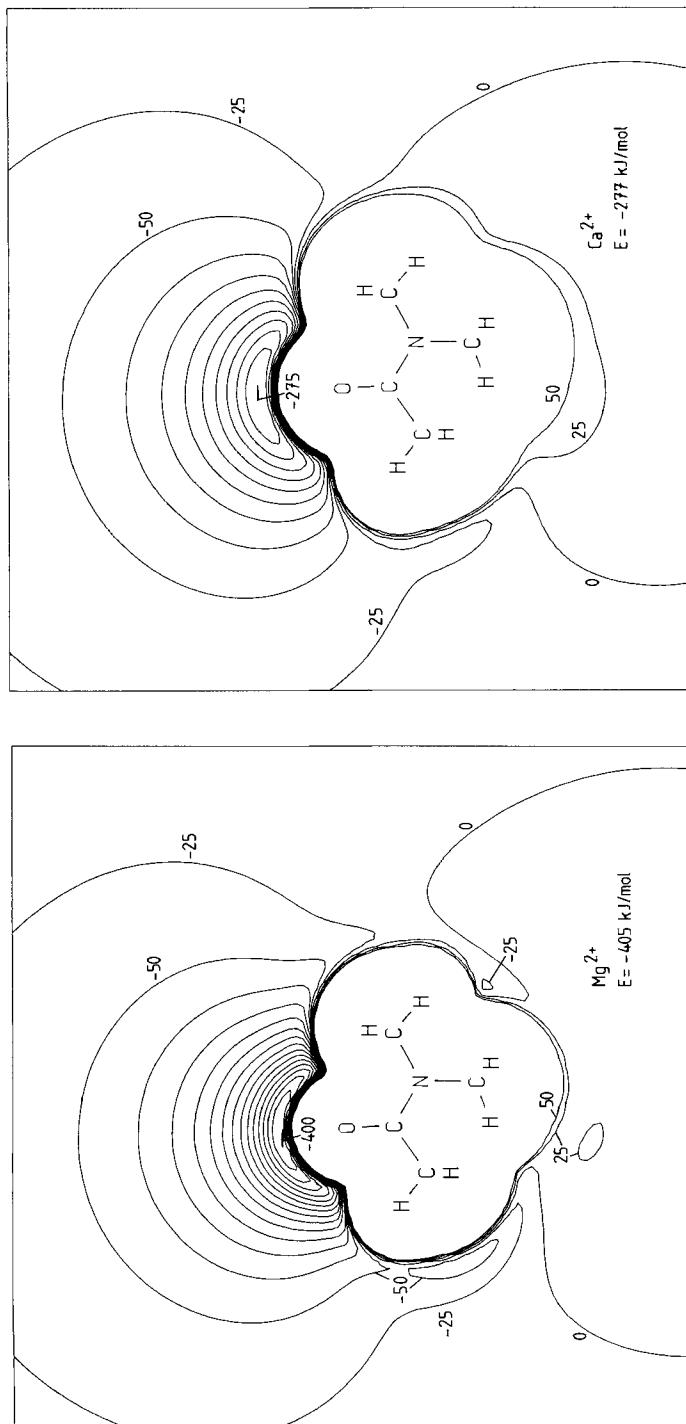


Fig. 2. Isoenergy contour diagrams for the interaction of Mg<sup>2+</sup> (left) and Ca<sup>2+</sup> (right) with N,N-dimethylacetamide in the symmetry plane of the molecule ( $z=0$  pm). The contour-to-contour interval is 25 kJ mol<sup>-1</sup>. The figure maps an area of 1800 pm square.

Table 3. Fitting constants for the atomic pair potentials for the interaction of  $Mg^{2+}$  with 19 classes of atoms studied (see also Fig. 1) and mean net charges of the atoms belonging to the individual classes<sup>a)</sup>

| Atom | Group | Nr. | Code                 | A               | B               | C               | Charge  |
|------|-------|-----|----------------------|-----------------|-----------------|-----------------|---------|
| H    | CH3   | 1   | HC(H2C)              | 0.16039471E+04  | 0.25420166E+05  | 0.56070685E-03  | 0.1826  |
|      |       | 2   | HC(H2C*)             | 0.11838410E+04  | 0.10793968E+05  | 0.15829639E+04  | 0.2037  |
| H    | CH2   | 3   | HC(H2N)              | 0.64344912E+03  | 0.8488108E+04   | 0.65868707E+03  | 0.1960  |
|      |       | 4   | HC(HC2)              | 0.47333516E+04  | 0.92309571E+05  | 0.19317752E+03  | 0.1950  |
| H    | NH2   | 5   | HC(HCC*)             | 0.18948385E+04  | 0.33047124E+05  | 0.16348130E+04  | 0.1876  |
|      |       | 6   | HC(HC*) <sup>2</sup> | 0.21958585E+04  | 0.17003733E+05  | 0.11904366E+04  | 0.2068  |
| C    | CH3   | 7   | HN(HC*)              | -0.50865361E+03 | 0.14794982E+05  | 0.11904366E+04  | 0.2998  |
|      |       | 8   | CH3 C(H2C)           | -0.71482191E+04 | 0.23978548E+05  | 0.12011504E+03  | -0.5514 |
| C    | CH2   | 9   | CH3 C*(=ON)          | 0.21196094E+05  | 0.45581292E+07  | 0.22841207E+04  | -0.6051 |
|      |       | 10  | CH3 N(CC*)           | 0.11745218E+05  | 0.19882029E+07  | 0.63715453E+03  | -0.4360 |
| C    | C*    | 11  | CH2 C(H3) C(H2C*)    | -0.33829079E+04 | 0.11992191E+07  | 0.31744084E-02  | -0.3551 |
|      |       | 12  | CH2 C(H2C) C*(=ON)   | 0.16811627E+05  | 0.33181748E+07  | 0.555778863E+03 | -0.3993 |
| C    | C*    | 13  | CH2 C*(=ON) C*(=ON)  | -0.12182399E+05 | 0.14066462E+06  | 0.39822767E+04  | -0.4641 |
|      |       | 14  | C*(H3) N(C2)=O       | 0.57266973E+04  | 0.23718824E+06  | 0.39666747E+04  | 0.4210  |
| N    | NH2   | 15  | C*(H2C) N(C2)=O      | 0.11762684E+05  | 0.48753681E+06  | 0.34301496E+04  | 0.4223  |
|      |       | 16  | C*(H2C*) N(H2)=O     | 0.33758351E+04  | 0.14602575E+06  | 0.39427092E+04  | 0.4273  |
| N    | N     | 17  | NH2 C*(=OC)          | 0.10661362E+05  | 0.363232426E+06 | 0.13867868E+04  | -0.6066 |
|      |       | 18  | NC(H3) C(H3) C*(=OC) | -0.48435106E+03 | 0.19202144E+06  | 0.15704710E+04  | -0.3254 |
| O    | O*    | 19  | O=C(CN)              | -0.10543587E+04 | 0.37372652E+05  | 0.25261112E+04  | -0.3990 |

a) The interaction energy  $I(L, Mg)$  is obtained according to Equation 1 in kJ mol<sup>-1</sup> if A, B and C are used as given in the table; the unit of  $r_M$  is [Å] and that of the net charges is e (atomic unit of electron charge). A pure Coulomb interaction corresponds to a value of  $C = 1389.354$ . The code contains the atomic symbols of the atoms (see column 1) followed by the atomic symbols of all  $\alpha$ - and  $\beta$ -neighbors ( $\beta$ -neighbors in parenthesis). X\* and X designate atoms participating in double bonds.

Table 4. Fitting constants for the atomic pair potentials for the interaction of  $\text{Ca}^{2+}$  with 19 classes of atoms studied (see also Fig. 1) and mean net charges of the atoms belonging to the individual classes<sup>a)</sup>

| Atom | Group | Nr. | Code                  | A               | B              | C               | Charge  |
|------|-------|-----|-----------------------|-----------------|----------------|-----------------|---------|
| H    | CH3   | 1   | HC(H2C)               | 0.13209518E+03  | 0.86627720E+05 | 0.15032460E-02  | 0.1826  |
|      |       | 2   | HC(H2C*)              | 0.62928916E+03  | 0.61857754E+05 | 0.15094100E+04  | 0.2037  |
|      |       | 3   | HC(H2N)               | -0.97388649E+02 | 0.10000000E+04 | 0.13241031E+04  | 0.1960  |
|      |       | 4   | HC(HC2)               | 0.66433109E+04  | 0.27360213E+06 | 0.24989022E+03  | 0.1950  |
|      |       | 5   | HC(HCC*)              | -0.22685345E+04 | 0.85656503E+05 | 0.62915987E-02  | 0.1876  |
| H    | NH2   | 6   | HC(HC*2)              | 0.42390168E+04  | 0.19729383E+06 | 0.10783285E+04  | 0.2068  |
|      |       | 7   | HN(HC*)               | 0.43186353E+04  | 0.65173846E+06 | 0.126218522E+04 | 0.2998  |
| C    | CH3   | 8   | CH3 C(H2C)            | 0.21951919E+05  | 0.74365125E+07 | 0.49420133E+02  | -0.5514 |
|      |       | 9   | CH3 C*(=ON)           | 0.15596090E+05  | 0.72818586E+07 | 0.22762369E+04  | -0.6051 |
|      |       | 10  | CH3 N(CC*)            | 0.76149498E+04  | 0.52968469E+07 | 0.17410043E+04  | -0.4360 |
|      |       | 11  | CH2 C(H3) C(H2C*)     | -0.21749254E+05 | 0.11706824E+07 | 0.3551          |         |
|      |       | 12  | CH2 C(H2C) C*(=ON)    | 0.51539587E+05  | 0.86873320E+07 | 0.58970843E+03  | -0.3993 |
|      |       | 13  | CH2 C*(=ON) C*(=ON)   | -0.24442900E+05 | 0.55289078E+06 | 0.33469235E+04  | -0.4641 |
|      |       | 14  | C* C(H3) N(C2)=O      | 0.86271720E+04  | 0.10160226E+07 | 0.43343097E+04  | 0.4210  |
|      |       | 15  | C* C(H2C) N(C2)=O     | -0.20534723E+04 | 0.51517495E+06 | 0.36207779E+04  | 0.4223  |
|      |       | 16  | C* C(H2C*) N(H2)=O    | 0.31393268E+05  | 0.62692364E+07 | 0.42060293E+04  | 0.4273  |
| N    | NH2   | 17  | NH2 C*(=OC)           | 0.28479565E+05  | 0.42389119E+07 | 0.14757465E+04  | -0.6066 |
|      |       | 18  | N C(H3) C(H3) C*(=OC) | 0.29413821E+04  | 0.12819185E+07 | 0.11411287E+04  | -0.3234 |
|      |       | 19  | O* =C(CN)             | -0.78867903E+04 | 0.15639239E+06 | 0.27317838E+04  | -0.3990 |

a) The interaction energy  $I(L, \text{Ca})$  is obtained according to Equation I in kJ mol<sup>-1</sup> if A, B and C are used as given in the table; the unit of  $r_{\text{M}}$  is [Å] and that of the net charges is e (atomic unit of electron charge). A pure Coulomb interaction corresponds to a value of C = 1389.354. The code contains the atomic symbols of the atoms (see column 1) followed by the atomic symbols of all  $\alpha$ - and  $\beta$ -neighbors (in parenthesis). X\* and =X designate atoms participating in double bonds.

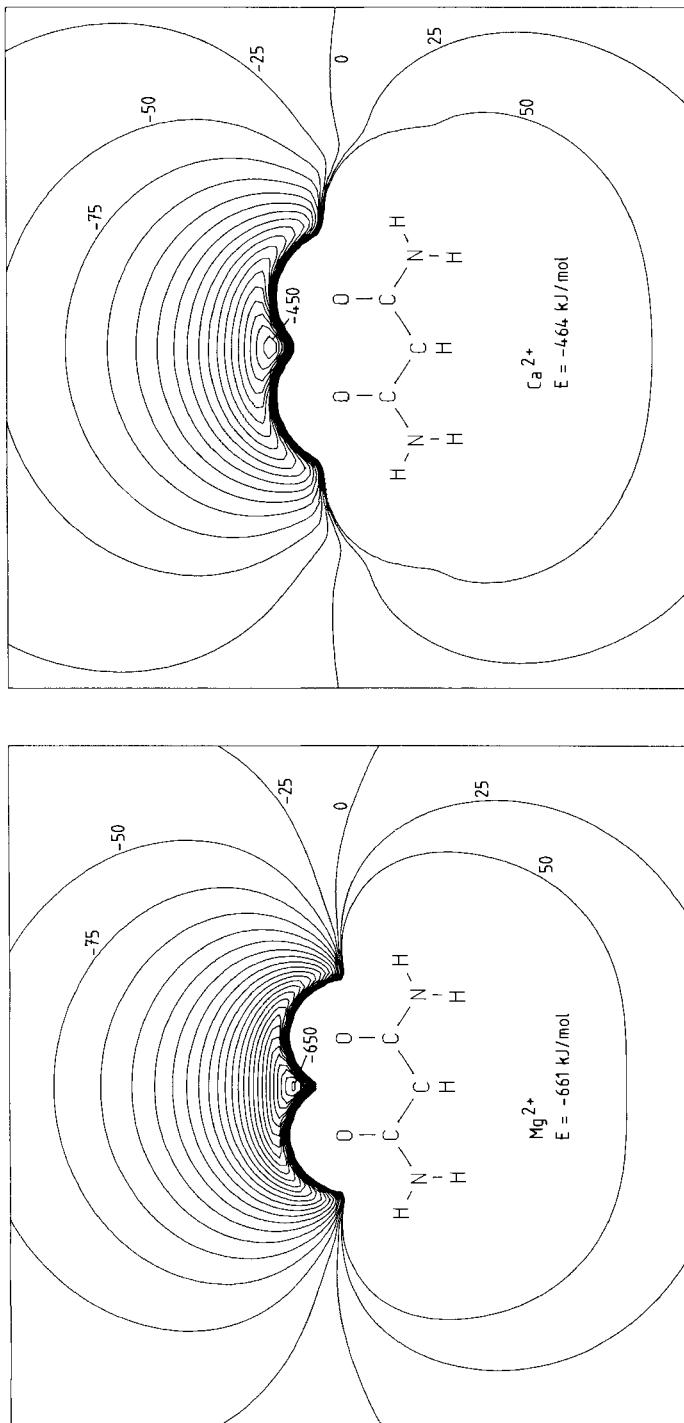


Fig. 3. Isoenergy contour diagrams for the interaction of  $\text{Mg}^{2+}$  (left) and  $\text{Ca}^{2+}$  (right) with malonamide ( $\theta(\text{OCCC}) = \theta(\text{CCCO}) = 0^\circ$ ) in the symmetry plane of the molecule ( $z = 0 \text{ pm}$ ). The contour-to-contour interval is  $25 \text{ kJ mol}^{-1}$ . The figure maps an area of  $1800 \text{ pm}^2$ .

Table 5. Number of SCF-LCAO-MO calculations performed for each structure (see Fig. 1) and standard deviation of the interaction energies approximated by Equation 1 with the parameters of Table 3 and 4 for  $Mg^{2+}$  and  $Ca^{2+}$ , respectively

| Structure                                       | Number of complexes        |           | Standard deviation      |           |
|---|----------------------------|-----------|-------------------------|-----------|
|   | (SCF-LCAO-MO calculations) |           | [kJ mol <sup>-1</sup> ] |           |
|   | $Mg^{2+}$                  | $Ca^{2+}$ | $Mg^{2+}$               | $Ca^{2+}$ |
| <i>N,N</i> -Dimethylacetamide                   | 95                         | 92        | 13.0                    | 12.6      |
| <i>N,N</i> -Dimethylbutyramide                  | 80                         | 84        | 13.1                    | 13.6      |
| Malonamide $\theta(OCCC)=\theta(CCCO)=0^\circ$  | 83                         | 83        | 20.1                    | 11.1      |
| Malonamide $\theta(OCCC)=\theta(CCCO)=45^\circ$ | 13                         | 12        | 17.4                    | 8.9       |
| Total   | 271                        | 271       | 15.8                    | 12.4      |

molecules (four structures) a total of 271 complexes with interaction energies lower than 120 kJ mol<sup>-1</sup> were considered for each ion. The fit by *Equation 1* led to the parameters presented in *Tables 3* and *4*. For the entire set of 271 calculations the least-square standard deviation was 15.8 and 12.4 kJ mol<sup>-1</sup> for  $Mg^{2+}$  and  $Ca^{2+}$ , respectively (see *Table 5*), which corresponds to 2.3–4.3% relative to the total interaction energy in the complexes of optimal ion location (see *Table 6*). In this table interaction energies derived by *ab initio* and pair-potential computations are compared. Entries A and B correspond to an optimization of the ion location by pair-potential and *ab initio* techniques, respectively.

Using the pair potentials given in *Tables 3* and *4* isoenergy contour diagrams were calculated for the energy of  $Mg^{2+}$  and  $Ca^{2+}$  in the field of *N,N*-dimethylacetamide (*Fig. 2*), malonamide (*Fig. 3*) and *N,N,N',N'*-tetramethylsuccinamide (*Fig. 4*, see also [24]). In contrast to the preferred location of  $Na^+$  and  $Mg^{2+}$  in the approximate direction of the O-lone-pairs of *N*-methylacetamide as obtained by

Table 6. Comparison of the interaction energies and optimal ion location derived by *ab initio* ( $E_{ab\ initio}$ ) and pair potential ( $E_{ABC}$ ) computations for the four structures studied for deriving pair potentials (fixed ligand geometry). A and B correspond to an optimization of the ion location by pair potentials respectively *ab initio* techniques.

| Structure                             | $Mg^{2+}$                                   |                                      |                                  |                      | $Ca^{2+}$                                   |                                      |                                  |                      |
|---------------------------------------|---|--------------------------------------|----------------------------------|----------------------|---|--------------------------------------|----------------------------------|----------------------|
|                                       | $E_{ab\ initio}$<br>kJ<br>mol <sup>-1</sup> | $E_{ABC}$<br>kJ<br>mol <sup>-1</sup> | Optimal ion<br>coordinates<br>pm | $d^a)$<br>Mg-O<br>pm | $E_{ab\ initio}$<br>kJ<br>mol <sup>-1</sup> | $E_{ABC}$<br>kJ<br>mol <sup>-1</sup> | Optimal ion<br>coordinates<br>pm | $d^a)$<br>Ca-O<br>pm |
| <i>N,N</i> -Dimethyl-<br>acetamide A  | –420  | –405                                 | –18/296/0                        | 175                  | –286  | –277                                 | –24/340/0                        | 219                  |
| B                                     | –421  | –404                                 | –22/299/0                        | 177                  | –286  | –277                                 | –26/339/0                        | 218                  |
| <i>N,N</i> -Dimethyl-<br>butyramide A | –431  | –420                                 | –5/296/0                         | 174                  | –294  | –287                                 | 2/340/0                          | 218                  |
| Malonamide<br>$\theta(OCCC)=$ A       | –670  | –661                                 | 0/250/0                          | 181                  | –483  | –464                                 | 0/304/0                          | 223                  |
| $\theta(CCCO)=0^\circ$ B              | –675  | –657                                 | 0/258/0                          | 187                  | –483  | –464                                 | 0/306/0                          | 225                  |
| Malonamide<br>$\theta(OCCC)=$ A       | –429  | –418                                 | –110/262/123                     | 176/<br>361          | –325  | –324                                 | 0/273/0                          | 240                  |
| $\theta(CCCO)=45^\circ$ B             |   |                                      | 110/262/–123                     |                      |   |                                      |                                  |                      |

a) Optimal ion-oxygen distances.

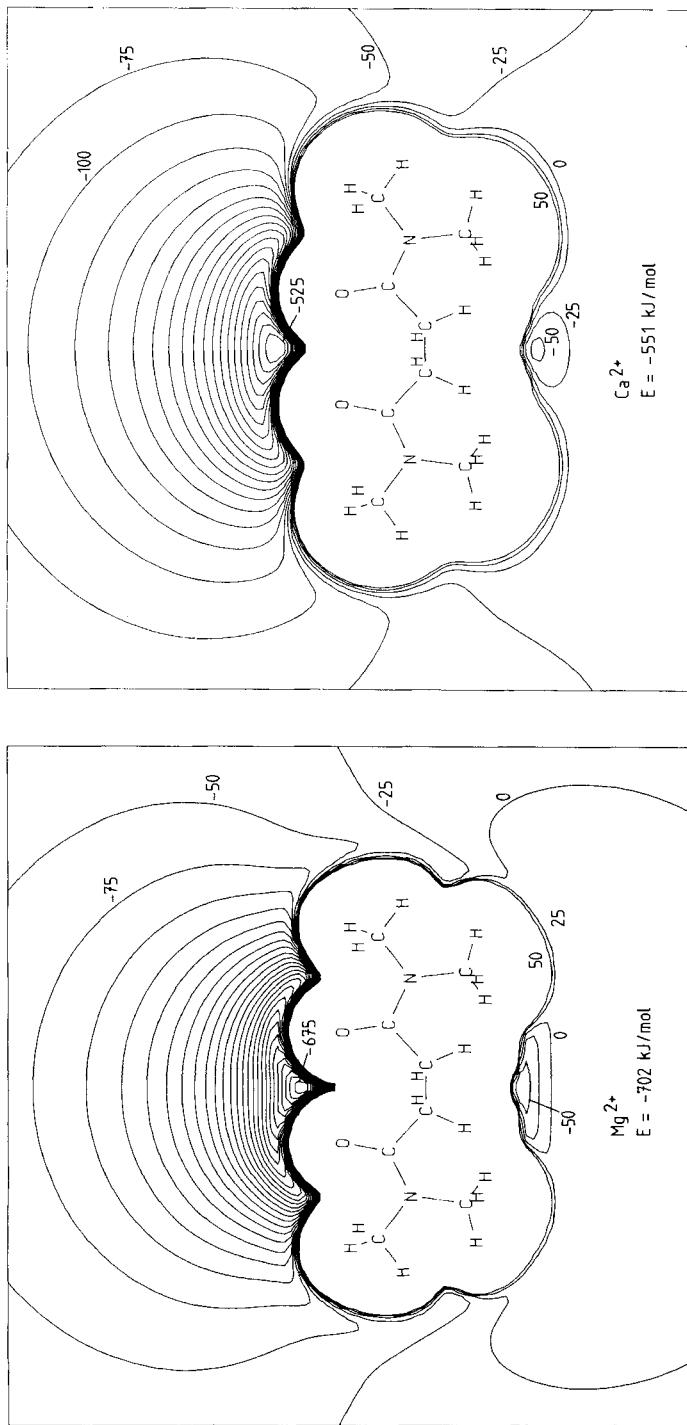


Fig. 4. Isoenergy contour diagrams for the interaction of  $\text{Mg}^{2+}$  (left) and  $\text{Ca}^{2+}$  (right) with  $\text{N},\text{N},\text{N}',\text{N}'\text{-tetramethylsuccinamide}$  ( $\theta(\text{OCCC}) = \theta(\text{CCCC}) = 60^\circ$ ,  $\vartheta(\text{CCCC}) = -90^\circ$ ). The plane of the diagrams is defined by the carbonyl-C-atoms and the  $C_2$ -axis of the molecule in this conformation. The contour to contour interval is  $25 \text{ kJ mol}^{-1}$ . The figure maps an area of  $1800 \text{ pm}^2$ .

Table 7. Comparison of the ion-ligand interaction energies obtained by the pair-potential method with ab initio results for some structures (fixed ligand geometry). For N-methylacetamide geometrical parameters of [22] [31] were used. The geometries of the remaining structures were fixed using the same parameters as for the four structures studied for deriving pair potentials (see Table 1, 2 and Table 4 of [11]). The net charges were determined by a Mulliken population analysis [32] for each structure.

| Structure                                 | Mg <sup>2+</sup>   |                                      |                                |   | Ca <sup>2+</sup>  |                                      |   |   |
|---|--|--------------------------------------|--------------------------------|---|---|--------------------------------------|---|---|
|   | $E_{ab\text{ initio}}$<br>kJ<br>mol <sup>-1</sup>                        | $E_{ABC}$<br>kJ<br>mol <sup>-1</sup> | Optimal ion location<br>$d^a)$ | $\alpha, \theta^b)$   | $E_{ab\text{ initio}}$<br>kJ<br>mol <sup>-1</sup>                                   | $E_{ABC}$<br>kJ<br>mol <sup>-1</sup> | Optimal ion location<br>$d^a)$  | $\alpha, \theta^b)$   |
| Malonamide                                | -270   | -316                                 | 177                            | $\alpha(\text{CO1Mg}) = 160^\circ - 165^\circ$<br>$\theta(\text{NCO1Mg}) = 0^\circ$   | -233  | 219                                  | $\alpha(\text{CO1Ca}) = 166^\circ$<br>$\theta(\text{NCO1Ca}) = 0^\circ$   |   |
| $\theta(\text{O1CCC}) = 0^\circ$          |  |                                      |                                |   |   |                                      |   |   |
| $\theta(\text{O2CCC}) = 180^\circ$        | -443   | -533                                 | 173                            | $\alpha(\text{CO2Mg}) = 173^\circ - 305^\circ$<br>$\theta(\text{NCO2Mg}) = 180^\circ$ | -403  | 212                                  | $\alpha(\text{CO2Ca}) = 176^\circ$<br>$\theta(\text{NCO2Ca}) = 180^\circ$ |   |
| N-Methyl-acetamide                        | c)<br>$\theta(\text{CNCO}) = 0^\circ$                                    | -414                                 | -417                           | 174   | $\alpha(\text{COMg}) = 179^\circ - 283^\circ$<br>$\theta(\text{NCOMg}) = 180^\circ$ | -222                                 | 220   | $\alpha(\text{COCa}) = 175^\circ$<br>$\theta(\text{NCOCa}) = 180^\circ$ |
|   | d)<br>$\theta(\text{CNCO}) = 0^\circ$                                    | -414                                 | -376                           | 175   | $\alpha(\text{COMg}) = 178^\circ - 283^\circ$<br>$\theta(\text{NCOMg}) = 180^\circ$ | -297                                 | 217   | $\alpha(\text{COCa}) = 179^\circ$<br>$\theta(\text{NCOCa}) = 0^\circ$   |
| <i>N,N,N',N'</i> -Tetramethyl-malonamide  | e)<br>$\theta(\text{OCCC}) = 0^\circ$<br>$\theta(\text{CCCO}) = 0^\circ$ | -691                                 | -721                           | 182   | on C <sub>2</sub> -axis   | -492                                 | -515  | 224 on C <sub>2</sub> -axis   |
| <i>N,N,N',N'</i> -Tetramethyl-succinamide |  | -705                                 | -702                           | 180   | on C <sub>2</sub> -axis   | -510                                 | -551  | 224 on C <sub>2</sub> -axis   |
| $\theta(\text{OCCC}) = 0^\circ$           |  |                                      |                                |   |   |                                      |   |   |
| $\theta(\text{CCCO}) = 60^\circ$          |  |                                      |                                |   |   |                                      |   |   |
| $\theta(\text{CCCC}) = -90^\circ$         |  |                                      |                                |   |   |                                      |   |   |

a) d: Optimal ion-oxygen distances in pm.

b) a: Optimal angle C=O....Mg, C=O.....Ca respectively; θ: Optimal dihedral angle N-C=O...Mg, N-C=O...Ca respectively.

c) N-atom described by class 18.

d) N-atom described by class 17.

e) Carbonyl-C-atoms described by class 16.

semiempirical methods (CNDO/2) [25] and to the results found for the interaction of Na<sup>+</sup> and K<sup>+</sup> with N-methylacetamide and methyl acetate as obtained by ab initio computations [26], the results in Figure 2 document a nearly colinear position relative to the carbonyl group. This is in agreement with recent findings for the interaction of Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup>, Be<sup>2+</sup>, and Mg<sup>2+</sup> with alkyl-substituted acetamide [27] and the Li<sup>+</sup>-complexes of formamide [28] and R<sub>2</sub>CO (R = NH<sub>2</sub>, CH<sub>3</sub>, OH, H, F) [29] [30].

For some structures not used in the derivation of the pair potentials the interaction energy for the optimal ion location (as obtained by the pair-potential method) is compared with values obtained by ab initio techniques for the same ion location (Table 7). Considering the fact that unsatisfactory atom classes [13] were used throughout the differences in the energies are, except for malonamide, acceptable (0.4 to 21.5%). For malonamide formally suitable atom classes are given in Tables 3 and 4; however, they do not cover the influence of a H-bond probably

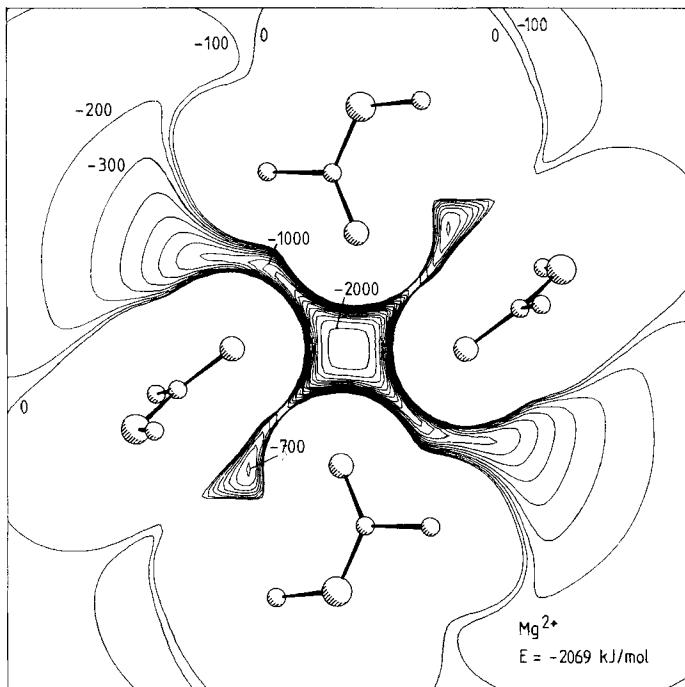


Fig. 5. Isoenergy contour map for the interaction of six *N*-methylacetamide molecules in octahedral arrangement with  $Mg^{2+}$  (two molecules are not depicted). The arrangement of the ligands corresponds to the structure of the  $Mg^{2+}$ -complex of *N*-methylacetamide  $[MgCl_2(C_3H_7ON)_6]$  [33] (see text). The net atomic charges calculated for a single *N*-methylacetamide molecule were used. The N-atoms were described by class 18. The plane of the diagram is defined by the four O-atoms (and the optimal location of the  $Mg^{2+}$ -ion. The contour-to-contour interval is  $100 \text{ kJ mol}^{-1}$ . The figure maps an area of  $1200 \text{ pm square}$ .

present in the conformation considered. If the assignment in atom classes as specified earlier [13] is accepted, this poses a clear limitation of the model used. The data presented in *Table 7* for *N*-methylacetamide document, however, that the ion location can be predicted nicely even if less than perfectly suited atom classes are used (see also [13]).

Based on the structure of the  $Mg^{2+}$ -complex of *N*-methylacetamide  $[MgCl_2(C_3H_7ON)_6]$  [33] the location of  $Mg^{2+}$  has been calculated by the pair-potential technique. The coordinates of all atoms other than H-atom for the six ligands were taken from X-ray structure analyses [33]. The positions of the H-atoms were calculated according to data published in [22] [31]. They do not agree with those available from [34], which are incomplete and partly erroneous. The isoenergy contour map for the interaction of the six *N*-methylacetamide ligands with  $Mg^{2+}$  is depicted in *Figure 5*. The location of the computed energy minimum agrees to better than  $0.01 \text{ pm}$  with the experimental value. The  $Mg^{2+}$  is neither located colinearly with the carbonyl group nor is it in the plane of the heavy atoms of the

ligand. The mean Mg-O distance is 206 pm in the array of six ligands and 174 pm in the 1:1-complex (see also *Fig. 13* in [33]). Therefore  $Mg^{2+}$  is located differently relative to a single ligand than to an array of ligands. A transfer of ion locations obtained from X-ray analysis of a 1:n-complex as optimal to a 1:1-complex is therefore problematic.

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